



## TEXTBOOK

James Stewart, Multivariable Calculus is a popular side reading for this course. Any edition works.

## ORGANISATION

Course head: Oliver Knill

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## MATHEMATICA

We have a computer algebra project in this course. Harvard has a site license for Mathematica. It is a professional and powerful software.

## SECTIONS

The course lectures (except reviews and intro meeting) are taught in sections. This assures you can discuss the material in class. Additional problem sessions are offered too. Lecture sections meet at:

MWF 9, MWF 10:30, MWF 12,  
MWF 1:30, MWF 3. Please section for one.

## MQC

Sun to Thu in 309, 8:30-10:30PM

## EXAM DATES

1. EXAM	2. EXAM	FINAL
OCT 1	NOV 5	DECEMBER
6 PM	6 PM	TBA
HALL C	HALL C	TBA

## GRADES

PART	PERCENTAGE
1. HOURLY	15
2. HOURLY	15
HOMEWORK	25
MATHEMATICA	5
FINAL	40

Harvard University Fall 2019

# MATH 21A

## SYLLABUS 2019

This standard multivariable calculus

course extends single variable calculus to higher dimensions. It provides a vocabulary for understanding fundamental processes like weather, planetary



motion, waves, heat and analysis in finance, life and social sciences. It teaches important background needed for statistics, computer graphics, bioinformatics, etc. It provides valuable tools for visualization as we study curves, surfaces, solids and other geometrical objects in two and three dimensions. It develops methods for solving optimization problems with and without constraints. You learn a powerful computer algebra system. The course enhances problem solving skills and prepares you for further study in any other fields of mathematics and its applications.

# CALENDAR

S	M	T	W	T	F	S
1	2	3	4	5	6	7
8	9	10	11	12	13	14
15	16	17	18	19	20	21
22	23	24	25	26	27	28
29	30	1	2	3	4	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30	31	1	2
3	4	5	6	7	8	9
10	11	12	13	14	15	16
17	18	19	20	21	22	23
24	25	26	27	28	29	30
1	2	3	4	5	6	7
8	9	10	11	12	13	14

# SYLLABUS

## 1. Vectors and Products

- coordinates and distance
- vectors and dot product
- cross product lines/planes

## 2. Functions and curves

- level surfaces quadrics
- curves, velocity acceleration
- arc length, curvature

## 3. Coordinates and Surfaces

- cylindrical coordinates
- spherical coordinates
- parametric surfaces

## 4. Partial derivatives

- \* review for first hourly

first midterm (week 1-3) Oct 1

- continuity
- partial derivatives

## 5. Linear approximation

- partial differential equations
- linear approximation
- chain rule implicit differentiation

## 6. Gradient

- \* Indigenous people day (no class)

- tangent spaces
- directional derivative

## 7. Extrema

- maxima, minima, saddle points
- Lagrange multipliers
- global extrema

## 8. Double integrals

- double integrals
- polar integration
- surface area

## 9. Triple integrals

- \* review for second midterm

second midterm (week 5-8)

Nov 5

- triple integrals
- spherical integrals

## 10. Line integrals

- vector fields
- line integrals
- line integral theorem

## 11. Stokes theorem

- Greens theorem
- curl, divergence and flux
- Stokes theorem

## 12. Divergence theorem

- Divergence theorem
- Thanksgiving (no class)
- Thanksgiving (no class)

## 13. Overview

- Overview, Outlook

Reading period (2-8) and Exam period (9-20)