

8. We use a  $u$ -substitution.

$$\begin{aligned}u &= 2x \\ du &= 2 dx \\ dx &= \frac{du}{2}\end{aligned}$$

$$V = \pi \int_0^{\frac{\pi}{4}} (\cos 2x)^2 dx$$

$$= \frac{1}{2} \pi \int (\cos u)^2 du \quad \text{We use } \cos^2 u = \frac{1 + \cos 2u}{2}$$

$$= \frac{1}{2} \pi \int \frac{1 + \cos 2u}{2} du$$

$$= \frac{1}{2} \pi \int \left[ \frac{1}{2} + \frac{\cos 2u}{2} \right] du$$

$$= \frac{1}{4} \pi u + \frac{1}{8} \pi \sin 2u \quad \text{We substitute } u = 2x \text{ back in.}$$

$$= \left[ \frac{1}{2} \pi x + \frac{1}{8} \pi \sin 4x \right]_0^{\frac{\pi}{4}}$$

$$= \frac{\pi^2}{8} + 0 - [0 + 0]$$

$$= \boxed{\frac{\pi^2}{8}}$$