

ADDITIONAL PROBLEMS

1. Assume that $f \in C^4(\mathbb{R})$, and $f'(0) \neq 0$. Show that there is a unique Möbius transform $\phi(x) = \frac{ax+b}{cx+d}$, such that

$$\lim_{x \rightarrow 0} \frac{\phi \circ f(x) - x}{x^3}$$

is finite. When the limit is finite, show that it equals to $\frac{Sf(0)}{6}$.

2. Assume that $Sf(x) < 0$ for all $x \in \mathbb{R}$, p is a one-sided attracting periodic point of f , and $W(p)$ is the maximal stable interval containing p . Assume that $W(p)$ is bounded. Show that for some i , there is a critical point of f in $W(f^i(p))$.