

Mathematics 116

Convexity and Optimization with Applications

Assignment I	Due in class on Tuesday, February 15.
Announcements	Sections begin next Monday. Details will be announced in class and on the web.
Reading	Study chapters 2 and 3 of Sundaram's FCOT. For background material, see also §1.2 and the Appendices. Read chapter 1 and glance through chapter 2 of Luenberger's OVSM. For those interested in finding out more about making rigorous arguments, the book <i>How to Read and Do Proofs</i> by Daniel Solow is a classic.
Exercises	From FCOT§1.7: #2, #16, #17, #26, #27, #32; §2.6: #3, #4; and §3.4: #5, #8.
Writing	In addition to handing these few paragraphs in with the other problems, you may also post your answers to the discussion section of the website (www.courses.fas.harvard.edu/~math116). <ol style="list-style-type: none">1. Find or think up another theoretical or applied problem related to convexity and optimization of interest to you and write up a brief description of it in the style of §1.2 of Luenberger or §2.3 of Sundaram.2. Find and describe another theoretical or applied situation where a vector space other than Euclidean n-space is important. Explain why it is important and give references. How do you know the space you found is actually different from \mathbf{R}^n?
Discussion	Please come to sections prepared to discuss the following questions. If you want to post your answers on the web site, please do so by Sunday. <ol style="list-style-type: none">1. What have you discovered so far about the Steiner Problem? Conditions for a solution in various cases? Interesting generalizations? What does the “dual” problem have to do with it?2. Why should you believe the Principle of Nested Closed Intervals? Is there such a principle for open intervals? How does PNCI generalize?
Words	Vocabulary to know includes: sup, inf, limit, continuous function, compact set, closed set, bounded set, sequence, subsequence, Weierstrass Theorem, Principle of Nested Closed Intervals.